

Multiple Choice (PART I)

- | | |
|-------|-------|
| 1. A | 21. D |
| 2. A | 22. A |
| 3. C | 23. C |
| 4. A | 24. B |
| 5. C | 25. D |
| 6. A | 26. C |
| 7. D | 27. C |
| 8. B | 28. C |
| 9. B | 29. D |
| 10. A | 30. B |
| 11. D | 31. B |
| 12. A | 32. C |
| 13. D | 33. B |
| 14. A | 34. B |
| 15. C | 35. D |
| 16. A | 36. B |
| 17. D | 37. B |
| 18. D | 38. C |
| 19. B | 39. C |
| 20. C | 40. C |

Part II- Constructed Response

Total Value : 60%

Answer ALL questions in the space provided. All necessary workings must be shown to receive full marks.

PART II Total Value: 60%

Value

41. a) (i) At what time(s) was the object stopped?

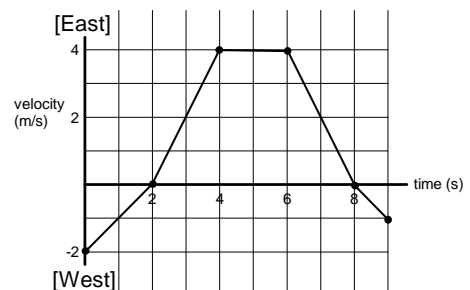
1 2 s and 8 s

(ii) Calculate the acceleration of the object between 2 s and 4 s.

0.5 $Acceleration = Slope = \frac{rise}{run}$

0.5 $= \frac{4\text{ m/s} - 0\text{ m/s}}{4\text{ s} - 2\text{ s}}$

1 $= \frac{4\text{ m/s}}{2\text{ s}} = 2\text{ m/s}^2 [E]$



(iii) Calculate the displacement between 0 s and 4 s.

$Displacement = Area$

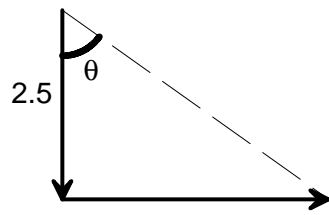
1 $Disp_{(0-2)} = \frac{1}{2}bh = \frac{1}{2}(2)(-2) = -2m$

1 $Disp_{(2-4)} = \frac{1}{2}(2)(4) = 4m$

1 $Disp_{(Total)} = 2m[E]$

b) A river flows at 2.5 m/s [S]. A boater heads 3.5 m/s [E]. Calculate the boater's resultant velocity with respect to the shore. Include a **labelled** vector diagram in your answer.

1 (diagram)



$${}_w v_g = 2.5 \frac{m}{s}, \quad {}_c v_w = 3.5 \frac{m}{s}$$

$${}_c v_g^2 = {}_c v_w^2 + {}_w v_g^2 \rightarrow {}_c v_g^2 = (3.5\text{ m/s})^2 + (2.5\text{ m/s})^2$$

1 ${}_c v_g^2 = 12.25 + 6.25 = 18.50 \rightarrow {}_c v_g = \sqrt{18.50} = 4.3\text{ m/s}$

$$\tan \theta = \frac{3.5}{2.5} = 1.4$$

1 $\theta = 54^\circ$

1 Resultant Velocity = $4.3\text{ m/s}[S\ 54^\circ\ E]$ or $4.3\text{ m/s}[E\ 36^\circ\ S]$.

(c) $v_1 = 0, a = 6.8 \text{ m/s}^2, t = 3.1 \text{ s}$

1.5 $v_2 = v_1 + at = 0 + (6.8 \text{ m/s}^2)(3.1 \text{ s}) = 21.08 \text{ m/s}$

The final velocity when accelerating is now the initial velocity when slowing down.

0.5 $v_1 = 21.08 \text{ m/s}, v_2 = 0 \text{ m/s}, a = -7.6 \text{ m/s}^2, \Delta d = ?$

$$v_2^2 = v_1^2 + 2a\Delta d$$

1.5 $\Delta d = \frac{v_2^2 - v_1^2}{2a} = \frac{0 - (21.08)^2}{2(-7.6)} = 29 \text{ m}$

0.5 The car travels 29 m before it stops so it will hit the garbage can.

42. a) Total Momentum Before = Total Momentum After

0.5 $\vec{P}_T = \vec{P}_P + \vec{P}_B$

0.5 $m_T \vec{v}_T = m_P \vec{v}_P + m_b \vec{v}_b$

1 $(80)(0) = 65\vec{v}_P + (15)(5.0)$

$$0 = 65\vec{v}_P + 75$$

1 $-75 = 65\vec{v}_P$

0.5 $-1.2 = \vec{v}_P$

0.5 **The velocity of the player is -1.2 m/s or 1.2 m/s [Left]**

b) A ship is being towed by two tugboats. Tugboat 1 exerts a force of $2.7 \times 10^3 \text{ N}$ [E 20.0° N] and tugboat 2 exerts a force of $2.7 \times 10^3 \text{ N}$ [E 20.0° S]. Calculate the net force exerted by the tugboats on the ship.

0.5 $F_{x1} = 2.7 \times 10^3 \text{ N} \cdot \cos 20.0^\circ = 2537 \text{ N}$

0.5 $F_{y1} = 2.7 \times 10^3 \text{ N} \cdot \sin 20.0^\circ = 923.5 \text{ N}$

0.5 $F_{x2} = 2537 \text{ N}$

0.5 $F_{y2} = -923.5 \text{ N}$

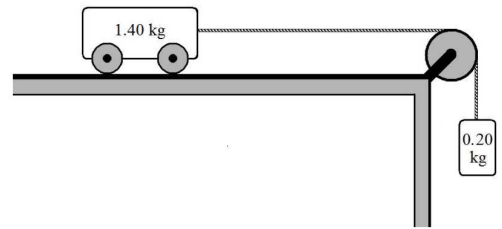


1 $F_{x(net)} = F_{x1} + F_{x2} = 2537 \text{ N} + 2537 \text{ N} = 5074 \text{ N}$

0.5 $F_{y(net)} = 0$

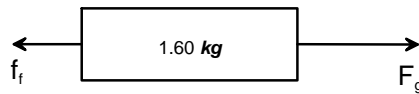
0.5 **The net force is 5074 N [E] or $5.1 \times 10^3 \text{ N}$ using significant digits.**

- c) A dynamics cart is connected to a 0.20 kg hanging mass by a massless string over a frictionless pulley. The force of friction between the cart and the table is 0.36 N.



One **possible** answer scheme is:

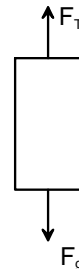
- 2 i) Calculate the magnitude of the acceleration of the system when the 0.20 kg mass is released.



1 $F_g = (0.20 \text{ kg}) \times 9.8 = 1.96 \text{ N}$
 1 $ma = 1.96 - F_T$
 $ma = 1.60 \text{ N}$
 $(1.60)a = 1.60 \text{ N}$
 $a = 1.0 \text{ m/s}^2$

- 2 ii) Calculate the tension in the string when the 0.20 kg mass is released.

1 (ii) $F_{net} = F_g - F_T$
 $F_{net} = 1.96 \text{ N} - 0.36 \text{ N}$
 $(0.20)(1.0) = 1.96 - F_T$
 $0.20 = 1.96 - F_T$
 $F_T = 1.8 \text{ N}$



* Other reasonable methods are also acceptable.

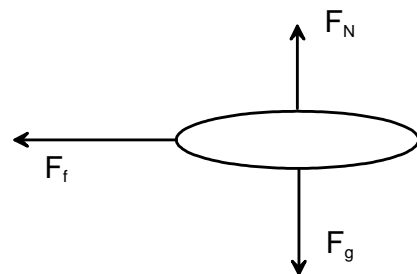
- d) A 1200 kg car is travelling along a highway where the posted speed limit is 25 m/s. The driver fully applies the brakes and comes to a stop, leaving a skid mark 83 m long. The coefficient of friction between the tires and the road is 0.45. Using physics, determine if the driver was speeding before he slammed on his brakes.

1 $F_f = \mu F_N$
 $ma = F_f$
 $F_f = (0.45)(1200)(9.8)$
 $a = -4.41 \text{ m/s}^2$

1 $F_{net} = F_f$
 $F_f = \mu mg$
 $(1200)a = -5292$
 $F_f = 5292 \text{ N}$

1.5 $v_2^2 = v_1^2 + 2a\Delta d$
 $v_1^2 = v_2^2 - 2a\Delta d$
 $v_1^2 = (0) - 2(-4.41)(83)$
 $v_1^2 = 732.06$
 $v_1 = 27 \text{ m/s}$

0.5 **The initial velocity was 27 m/s so the car was speeding.**



43. (a) A 5.00×10^2 kg roller coaster travels at a speed of 15.0 m/s when at a height of 5.00 m above the ground (assume mechanical energy is conserved).

i) Calculate the kinetic energy at 5.00 m.

1
$$E_k = \frac{1}{2}mv^2 = \frac{1}{2}(5.00 \times 10^2)(15.0\text{m/s})^2 = 5.63 \times 10^4\text{J}$$

ii) Calculate the gravitational potential energy at 5.00 m.

1
$$E_g = mgh = (5.00 \times 10^2)(9.8\text{m/s}^2)(5.00\text{m}) = 2.45 \times 10^4\text{J}$$

iii) Calculate the speed of the roller coaster when it is at a height of 10.0 m.

1
$$E_T = E_k + E_g = 56300\text{J} + 24500\text{J} = 80800\text{J}$$

$$E_k = E_T - E_g = 80800\text{J} - (500)(9.8)(10.0)$$

1
$$= 31500\text{J}$$

$$E_k = \frac{1}{2}mv^2$$

1
$$v = \sqrt{\frac{2E_k}{m}} = \sqrt{\frac{2 \times 31750}{500}} = 11.3 \text{ m/s}$$

- b) A 605 kg race car accelerates from 20.0 m/s to 60.0 m/s.

i) Calculate the work done during the acceleration.

0.5
$$W = \Delta E = \frac{1}{2}mv_2^2 - \frac{1}{2}mv_1^2$$

$$W = \frac{1}{2}(605)(60.0)^2 - \frac{1}{2}(605)(20.0)^2$$

2
$$W = 1.09 \times 10^6 - 1.21 \times 10^5$$

0.5
$$W = 9.68 \times 10^5\text{J}$$

ii) If the car generates 582 kW of power, calculate the time it took to accelerate.

1
$$t = \frac{W}{P} = \frac{9.68 \times 10^5}{582 \text{ kW}}$$

0.5
$$t = \frac{9.68 \times 10^5}{582 \text{ kW} \times \frac{1000\text{W}}{1\text{kW}}}$$

0.5
$$t = 1.66 \text{ s}$$

- c) A horizontal spring having a spring constant of 40.0 N/m undergoes simple harmonic motion when a 1.20 kg mass stretches it 20.0 cm from its rest position. Calculate the speed of the mass when it is 5.00 cm from the rest position.

1
$$E_{Total} = E_e = \frac{1}{2}kx^2 = \frac{1}{2}(40.0)(0.200)^2 = 0.800J$$

At 5.00 cm,

1
$$E_e = \frac{1}{2}kx^2 = \frac{1}{2}(40.0)(0.0500)^2 = 0.0500 J$$

0.5
$$E_{Total} = E_e + E_k$$

$$0.800J = 0.0500J + E_k$$

0.5
$$E_k = 0.750 J$$

$$E_k = \frac{1}{2}mv^2$$

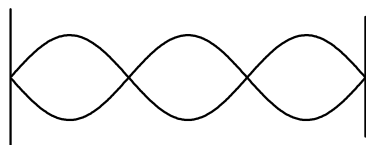
0.5
$$0.750 = \frac{1}{2}(1.20)v^2$$

0.5
$$v = 1.12 m/s$$

44. a) A bass guitar string is 1.3 m long and vibrating in the third harmonic.

- i) Sketch the standing wave pattern described above.

1



- ii) Find the frequency if the speed of the wave is 181 m/s.

$$L = 1.5\lambda$$

$$1.3 = 1.5\lambda$$

1
$$\lambda = 0.87m$$

1
$$f = \frac{v}{\lambda} = \frac{181 m/s}{0.87 m} = 210 Hz$$

- b) A 310 Hz tuning fork is held over the mouth of a close-end air column. If the speed of sound is 352 m/s, determine the length of the air column which produces the second resonant sound.

1
$$L = \frac{3}{4}\lambda$$

$$v = f\lambda$$

1
$$\lambda = \frac{v}{f} = \frac{352 m/s}{310 Hz} = 1.135 m$$

1
$$L = \frac{3}{4}\lambda = \frac{3}{4}(1.135) = 0.85 m$$

- c) An ambulance siren emits a frequency of 440 Hz. If the air temperature is 22°C, calculate the frequency heard by an observer if the ambulance is coming toward him at 26 m/s.

1 $v = 332 + 0.6T = 332 + 0.6(22) = 345.2 \text{ m/s}$

1.5 $f = \frac{f_0 v_s}{v_s - v_0} = \frac{(440 \text{ Hz})(345.2 \text{ m/s})}{345.2 \text{ m/s} - 26 \text{ m/s}}$

1 $f = \frac{151888}{319.2} = 475.8 \text{ Hz}$

0.5 $f = 480 \text{ Hz}$

- d) A light with a wavelength of $5.50 \times 10^{-7} \text{ m}$ is shone through two slits which are $3.0 \times 10^{-6} \text{ m}$ apart. Calculate the angle at which the first order maxima occur.

0.5 $n\lambda = d \sin \theta$

1 $(1)(5.50 \times 10^{-7}) = (3.0 \times 10^{-6})(\sin \theta)$

1 $\sin \theta = \frac{(5.50 \times 10^{-7})}{(3.0 \times 10^{-6})} = 0.1833$

0.5 $\theta = 11^\circ$

- e) A student is standing at the edge of a pool that is 2.3 m deep. A set of keys is at the bottom of the pool, 3.2 m from the wall. The index of refraction for air is 1.0 and for water is 1.3. What is the angle of refraction in air?

$\tan \theta = \frac{1.2}{2.3} = 0.5217$

1 $\theta = 27.6^\circ$

$n_1 \sin \theta_1 = n_2 \sin \theta_2$

1 $1.3(\sin 27.6) = 1.0(\sin \theta_2)$

1 $\theta_2 = 37^\circ$

